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Review of Scientific Instruments

Volume 82

Number 7

Page range 73707

Year 2011-07-01

URL http://hdl.handle.net/2297/29300
doi: 10.1063/1.3608447

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Wideband phase-locked loop circuit with real-time phase correction for frequency modulation atomic force microscopy

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(Received 20 April 2011; accepted 16 June 2011; published online 20 July 2011)

We have developed a wideband phase-locked loop (PLL) circuit with real-time phase correction for high-speed and accurate force measurements by frequency modulation atomic force microscopy (FM-AFM) in liquid. A high-speed operation of FM-AFM requires the use of a high frequency cantilever which, however, increases frequency-dependent phase delay caused by the signal delay within the cantilever excitation loop. Such phase delay leads to an error in the force measurements by FM-AFM especially with a low Q factor. Here, we present a method to compensate this phase delay in real time. Combined with a wideband PLL using a subtraction-based phase comparator, the method allows to perform an accurate and high-speed force measurement by FM-AFM. We demonstrate the improved performance by applying the developed PLL to three-dimensional force measurements at a mica/water interface. © 2011 American Institute of Physics. [doi:10.1063/1.3608447]

I. INTRODUCTION

Frequency modulation atomic force microscopy (FM-AFM)1 has widely been used for atomic-scale studies on various materials in vacuum.2,3 In addition, recent advances in FM-AFM instrumentation4 has enabled its operation in liquid with true atomic resolution,5 which has stimulated subsequent studies on biological systems by FM-AFM.6–10 However, biological systems have much larger fluctuations, corrugations, and inhomogeneity than those of the typical samples that have been studied by FM-AFM in vacuum. Therefore, non-destructive imaging of biological systems requires to enhance the operation speed of FM-AFM. Although molecular-scale imaging of relatively simple biological systems have been realized even with a present FM-AFM system,6–10 a large part of the biological systems and phenomena have remained inaccessible by FM-AFM due to the insufficient operation speed.

The improvement of the operation speed in FM-AFM requires to enhance the resonance frequency or the bandwidth of each component constituting the tip-sample distance feedback loop. In particular, the enhancement of the cantilever resonance frequency (ω0 ≡ 2πf0) is essential as it determines the theoretical limit of the operation speed and the force sensitivity in FM-AFM.1 Owing to the recent progress in the micromachining technologies, small cantilevers with a megahertz order f0 has become commercially available. In contrast, knowledge on the instrumentation and techniques required for using such a high frequency cantilever has not been established especially for the FM-AFM operation in liquid.

In FM-AFM, the cantilever excitation frequency (ω ≡ 2πf) is regulated with a feedback control circuit such that the phase difference between the cantilever excitation and the deflection signals is kept constant. This feedback control operates based on the assumption that the frequency-dependent phase change in the frequency range around f0 is caused only by the cantilever. However, in the case of FM-AFM with a low Q factor and a high frequency cantilever, the frequency-dependent phase delay (Δφd) caused by other components in the feedback loop is not necessarily negligible, which leads to an error in the measurements of conservative and dissipative forces by FM-AFM.11,12

Recently, it has become common to use a phase-locked loop (PLL) circuit for producing a cantilever excitation signal as well as for the detection of the frequency shift (Δf) of the cantilever oscillation in FM-AFM.13 In the previous study, we have presented a design for a high-speed digital PLL with a subtraction-based phase comparator (S-PLL).14 The developed S-PLL has a detection bandwidth of 100 kHz, which is much higher than that of a commonly used digital PLL with a multiplication-based phase comparator (M-PLL). However, accurate cantilever excitation with the S-PLL has remained difficult mainly due to the error caused by Δφd. In addition, the effects of the improved operation speed obtained by the S-PLL has not been experimentally demonstrated in FM-AFM measurements.

In this study, we have developed a digital S-PLL with a real-time phase correction circuit for an accurate cantilever excitation and a high-speed Δf detection. First, we describe the mechanism causing Δφd in FM-AFM. Second, we propose to combine a real-time phase correction circuit with an S-PLL to compensate Δφd. Third, we demonstrate the effect of the phase correction circuit by comparing the phase versus frequency curves obtained by PLLs with different designs. Finally, we demonstrate the improved performance of the developed S-PLL in a high-speed measurement of three-dimensional force distribution at a mica/water interface.

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II. FREQUENCY-DEPENDENT PHASE DELAY

In this section, we describe the mechanism causing $\Delta \phi_d$ in an FM-AFM setup to clarify the problem to be solved in this study. Figure 1(a) shows a typical FM-AFM setup using a PLL for the cantilever excitation. In this setup, a cantilever deflection signal is fed into a PLL which produces $\Delta f$ and cantilever excitation signals. The phase and amplitude of the excitation signal is adjusted by a phase shifter (PS) and an AGC and an actuator as “the cantilever excitation loop.”

The PLL consists of a phase comparator (PC), a loop filter (LF), and a voltage controlled oscillator (VCO). Among them, the PC is shared with the cantilever excitation loop while the LF and the VCO are implemented outside. The PC compares the phase of the PLL input ($v_a$) and the VCO output ($v_b$) signals and outputs their difference ($\phi_{PC}$). This signal is filtered by the LF and fed into the VCO which outputs a sine wave whose frequency ($\omega$) changes in proportion to the input signal ($\Delta \omega$) with an offset frequency of $\omega_0$ (i.e., $\omega \equiv \omega_0 + \Delta \omega$). The VCO output is routed back to the PC. This loop works to adjust $\omega$ such that $\phi_{PC}$ is kept constant. As a result, $\omega$ is regulated to equal the frequency of the PLL input.

In the basic principle of FM-AFM, $\omega$ is adjusted to keep the phase delay caused by the cantilever ($\phi_{CL}$) at $-90^\circ$. Namely, the phase difference between $v'_a$ and $v'_b$ in Fig. 1(b) is kept constant. However, in a typical FM-AFM setup, the phase difference between $v_a$ and $v_b$ (i.e., $\phi_{PC}$) is kept constant. In the setup, there are several components between $v'_a$ and $v_a$ and between $v'_b$ and $v_b$ such as a cantilever deflection sensor and an actuator for the cantilever excitation. The signal delay caused by these components ($\tau_d$) leads to a phase delay $\phi_d$ given by

$$\phi_d = \tau_d \omega = \tau_d \omega_0 + \tau_d \Delta \omega \equiv \phi_0 + \Delta \phi_d. \quad (1)$$

In the right side of this equation, the first term $\phi_0 \equiv \tau_d(\omega_0)$ is constant and hence can be compensated with a PS as shown in Fig. 1(b). In contrast, the second term $\Delta \phi_d \equiv \tau_d(\Delta \omega)$ varies in proportion to $\Delta \omega$ during FM-AFM measurements, which cannot be compensated with a constant PS. Owing to the frequency-dependent phase delay $\Delta \phi_d$, $\phi_{CL}$ is not kept constant and shows deviation from $-90^\circ$. As the quantitative interpretation of the conservative and dissipative forces measured by FM-AFM is based on the assumption that $\phi_{CL}$ is kept at $-90^\circ$, the variation of $\phi_{CL}$ gives rise to an error in such an interpretation.

The influence from $\Delta \phi_d$ is particularly serious when a high frequency cantilever is used in liquid. $\Delta \phi_d$ increases with increasing $\Delta \omega$ while $\Delta \omega$ increases with increasing $\omega_0$. Thus, the use of a high frequency cantilever results in a large $\Delta \phi_d$. In addition, the Q factor ($Q$) of the cantilever resonance in liquid is much lower than that in air or in vacuum. With a low Q factor, $\phi_{CL}$ shows small frequency dependence around $f_0$ so that the phase change caused by $\Delta \phi_d$ is not negligible. Consequently, the influence from $\Delta \phi_d$ is more evident in liquid than that in air or in vacuum.

III. REAL-TIME PHASE CORRECTION

In this section, we present a PLL design that allows to solve the problem caused by $\Delta \phi_d$. We first introduce the designs for the cantilever excitation circuits using an M-PLL and an S-PLL. Then, we propose a design for an S-PLL with a real-time phase correction circuit, which enables to compensate the frequency-dependent phase change caused by $\Delta \phi_d$.

Figures 2(a) and 2(b) show designs for the cantilever excitation circuits with an M-PLL and an S-PLL, respectively. In an M-PLL, a multiplication-based PC is used for the detection of $\phi_{PC}$, where two input sine waves are multiplied to produce $2\omega$ and DC components. While the $2\omega$ component is suppressed by low pass filter (LPF), the DC component is used as a phase signal. In this design, the use of a LPF in the PLL significantly reduces the PLL bandwidth ($B_{PLL}$). In contrast, S-PLL is free of this problem owing to the use of a subtraction-based PC, where the phase of the PLL input signal is compared with that of the signal from the phase-output VCO ($\phi$-VCO) by subtraction. Owing to the linear subtraction process, no higher harmonics are generated and hence no LPF is required. Thus, the S-PLL design is more suitable for a high-speed $\Delta f$ detection than the M-PLL design.

However, one drawback of the S-PLL design is an increase of the delay components in the cantilever excitation loop. In the S-PLL design, non-linear signal processing units such as a phase detector and a cosine wave generator are not implemented in the PLL but in the cantilever excitation loop. Although this is the major reason for the wide bandwidth obtained by this design, these additional delay components increase $\Delta \phi_d$. Therefore, the problem caused by $\Delta \phi_d$ is more serious in the S-PLL design than that in the M-PLL design.

To solve this problem, we propose a design for an S-PLL with a real-time phase correction circuit [Fig. 2(c)]. In this design, the PLL output ($\Delta \omega$) is multiplied by $\tau_d$ to obtain a signal corresponding to $\Delta \phi_d(=\tau_d \Delta \omega)$. The obtained signal is subtracted from the output of the phase detector to cancel...
FIG. 2. (Color online) Block diagrams showing the cantilever excitation setups with different PLL designs. (a) M-PLL. (b) S-PLL. (c) S-PLL with a phase correction circuit.

out $\Delta \phi_d$. In this way, the design enables cantilever excitation without the influence from $\Delta \phi_d$.

Although it is also possible to develop an M-PLL with a phase correction circuit, such a PLL is probably too slow to be used in many of the applications. The phase correction circuit is a feedback loop consisting of a PLL, a multiplier, a LPF, and a PS as shown in Fig. 2(c). To ensure the stability of the loop, the cutoff frequency of the LPF ($f_{LPF}$) should be set at a value sufficiently lower than $B_{PLL}$. For the developed S-PLL having $B_{PLL}$ on the order of megahertz, we use $f_{LPF}$ of 10 kHz to ensure the stability. Thus, for a typical M-PLL having $B_{PLL}$ on the order of kilohertz, we expect that $f_{LPF}$ should be set at $\sim 10$ Hz, which is too slow for many of the applications.

IV. EXPERIMENTAL DETAILS

The S-PLLs with and without the phase correction circuit were implemented in a field programmable gate array (FPGA) chip (Virtex-4 SX: Xilinx). 14-bit ADCs (AD6645: Analog Devices) and DACs (AD9772: Analog Devices) were used for the signal conversions. The FPGA, ADCs, and DACs were driven at a clock frequency of 20 MHz.

For the purpose of comparison, we used a commercially available M-PLL (OC4: Nanonis). The ADCs and DACs of this PLL are driven at a clock frequency of 40 MHz, which is twice as high as that for the S-PLL used in this study.

The AFM experiments were performed with a custom-built FM-AFM with a low noise cantilever deflection sensor and a photothermal cantilever excitation system. A commercially available AFM controller (ARC2: Asylum Research) was used with some modifications in the software. The AFM experiments were performed at room temperature. The measurements of the $\phi_{PC}$ versus frequency curves were performed in pure water while the 3D imaging was performed in phosphate buffer saline (PBS) solution. The sample for the 3D imaging was prepared by cleaving a mica disc (01877-MB: SPI Supplies) and depositing 150 $\mu$l of PBS solution onto the surface.

V. PHASE VERSUS FREQUENCY CURVES

Figure 3(a) shows $\phi_{PC}$ versus frequency curves measured by the S-PLLs with and without the phase correction circuit. A band pass filter (BPF) was used as a model of a cantilever...
In the frequency range around $f_0$, a phase curve shows almost linear dependence on the frequency as shown in Fig. 3(c). From the slope of a phase curve in this frequency range, an apparent Q factor ($Q_a$) can be calculated based on the following equation:

$$Q_a = \frac{\Delta f}{\Delta f / \Delta f} \bigg|_{f_0}$$

The $Q_a$ values calculated with the phase curves obtained with the M-PLL and the S-PLL are 7.7 and 6.2, respectively. Compared to the true Q factor estimated from the thermal vibration spectrum ($Q = 6.3$), these values contain $+22.2\%$ and $-1.6\%$ errors, respectively. This result shows that the increase of $Q_a$ caused by $\Delta \phi$ can be greatly suppressed by the S-PLL with the phase correction circuit. As the increase of $Q_a$ directly leads to an error in the interpretation of the measured conservative and dissipative forces, the suppression of $Q_a$ is essential for an accurate force measurements by FM-AFM.

VI. 3D HYDRAULIC FORCE MEASUREMENTS

We have performed measurements of 3D force distribution at a mica/water interface by 3D scanning force microscopy (3D-SFM) (Ref. 18) using the M-PLL and the S-PLL with the phase correction circuit. In 3D-SFM, the vertical tip position ($z_t$) is modulated with a frequency ($f_m$) faster than the bandwidth of the distance regulation while the tip is laterally scanned. During the scan, $\Delta f$ is recorded in real time with respect to the 3D tip position while the averaged tip height is regulated to keep the averaged $\Delta f$ value constant. In this technique, a high-speed FM detector is required for the real time recording of the $\Delta f$ variation induced by the fast modulation of the tip height. Thus, this application is suitable for testing the effect of the enhanced bandwidth obtained by the S-PLL.

Figures 4(a) and 4(b) show Z cross sections derived from the 3D $\Delta f$ images obtained by the M-PLL and the S-PLL with the phase correction circuit, respectively. The image obtained with the S-PLL shows a clearer contrast than that obtained by the M-PLL due to the enhanced $B_{PLL}$. This difference is particularly evident in the contrasts corresponding to a hydration layer. While the image obtained by the S-PLL shows a layer-like contrast near the mica surface, the image obtained by the M-PLL shows a vague and broad contrast at the corresponding position.

This difference is also confirmed in the $\Delta f$ versus distance curves [Fig. 4(c)] obtained by averaging the images shown in Figs. 4(a) and 4(b). The curve obtained with the S-PLL shows a clear peak corresponding to the hydration layer as indicated by the arrow while such a peak is hardly seen in the curve obtained with the M-PLL. These results demonstrate that the S-PLL has an advantage over the M-PLL in the high-speed imaging of 3D hydration structure.

The image obtained by the M-PLL shows a bright contrast at a region far from the surface [region (i) in Fig. 4(a)]. Since this region corresponds to the bulk water, it should show a uniform $\Delta f$ distribution as seen in the image obtained by the S-PLL. Thus, the bright contrast found in Fig. 4(a) should be a measurement error. Here, we explain the mechanism causing
During the 3D-SFM imaging, $z_i$ is modulated with a sine wave as shown in Fig. 4(d). In response to the tip approach and retract, $\Delta f$ should show a sharp increase and decrease near the sample surface, respectively. Thus, if the PLL response is sufficiently fast, the $\Delta f$ signal should change as illustrated by a solid line in Fig. 4(d). However, if the PLL response is too slow, the $\Delta f$ signal may exhibit a significant delay as illustrated by a dotted line in Fig. 4(d).

As the images shown in Figs. 4(a) and 4(b) were obtained by recording the $\Delta f$ signal during the tip approach processes, the transient $\Delta f$ response indicated by circles (i) and (ii) in Fig. 4(d) should lead to an error in the obtained image and the force curve. In fact, the bright contrast found in region (i) in Fig. 4(a) corresponds to the error indicated by circle (i) in Fig. 4(d). This error is also confirmed in the force curve shown in Fig. 4(c) as indicated by circle (i). Similarly, the error indicated by circle (ii) in Fig. 4(d) accounts for the delayed $\Delta f$ response indicated by circle (ii) in Fig. 4(c). These results demonstrate that the improved $B_{PLL}$ obtained by the S-PLL is essential for an accurate and high-speed force measurement by FM-AFM in liquid.

Although the imaging speed of 3D-SFM is not determined only by $B_{PLL}$, here we describe the improvement that we observed in the case of our experimental setup. With the setup using the M-PLL, the fastest imaging speed that allows to obtain an image without a significant distortion was 53 s per 3D image ($f_m = 200$ Hz, 0.32 s per XZ image) as reported previously. With the developed S-PLL using the real-time phase correction circuit, we have been able to obtain a 3D image in 13 s ($f_m = 781$ Hz, 0.082 s per XZ image) as shown in Fig. 4(b). This is an improvement by a factor of four. In addition, the present imaging speed is not limited by the PLL bandwidth but by the data acquisition speed. As the developed PLL has $B_{PLL}$ higher than 100 kHz, we expect that it should allow imaging with $f_m$ higher than a few kilohertz. This corresponds to the imaging speed faster than 10 s per 3D image.

ACKNOWLEDGMENTS

This work was supported by PRESTO, Japan Science and Technology Agency.